Acc. Geom/Algebra II
Graphing Rational Functions Worksheet \#1

Name $\qquad$
$\qquad$ Date $\qquad$

1. Consider the function $f(x)=x^{2}$.
A) Sketch this function to the right.
B) What is its domain? $\qquad$
C) What is its range? $\qquad$
D) What are coordinates of its vertex? $\qquad$
2. Consider the function $g(x)=\frac{1}{x}$.
A) Sketch this function to the right.
B) What is its domain? $\qquad$
C) What is its range? $\qquad$
D) An asymptote is a line that a graph gets very close to. What are equations of the asymptotes of this graph?


3. Consider the equation of $f(x)$, if it is translated up 4 units and to the right 3 units.
A) Write the equation of this new function. $\qquad$
B) How can we tell from the equation that is has been moved? $\qquad$
C) What is the new domain? $\qquad$
D) What is the new range? $\qquad$
E) What are coordinates of the new vertex?
4. Consider the equation $h(x)=4+\frac{1}{x-3}$.
A) Graph this function in the space to the right.
B) How is it like $g(x)$ ? $\qquad$
C) How is it different from $g(x)$ ?
D) What is the new domain? $\qquad$
E) What is the new range? $\qquad$

F) What are equations of the asymptotes?
5. Consider the function $\mathrm{j}(\mathrm{x})=\frac{3 x-4}{x+2}$.
A) Graph this function in the space to the right.
B) How is it like $g(x)$ ? $\qquad$
C) How is it different from $g(x)$ ? $\qquad$
D) Divide this function and write the quotient.

E) Use the above quotient to describe the transformations on $g(x)$.
F) What is the domain? $\qquad$
G) What is the range? $\qquad$
H) What are equations of the asymptotes?
6. Consider the function $F(x)=\frac{x^{2}-x-6}{x-3}$
A) Graph this function in the space to the right.
B) Why doesn't it appear to have asymptotes?
C) Factor the numerator and simplify this function.
D) What is the domain? $\qquad$
E) What is the range? $\qquad$

$F(3)$ is undefined (actually, it is called indeterminate form) when $x=3$. The point $(3,5)$ is described as a "removable discontinuity" in calculus, but we shall describe it as a hole in our graph. How could we algebraically get that $\boldsymbol{y}$-value from our equation?
7. For each of the following: a) find the domain of the function, b) divide to write the function in transformational form, c) find equations of all the asymptotes, d) describe the transformations on $y=1 / x$ that have been done to this function and, e) sketch the graph.
A) $f(x)=\frac{5}{x-2}$
B) $f(x)=\frac{-2 x+5}{x+1}$
C) $f(x)=\frac{3 x-2}{x}$
