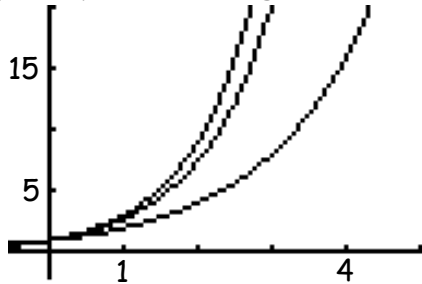
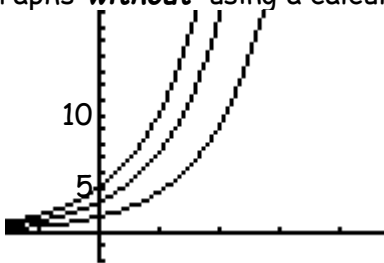


Analyzing Graphs of Exponential Functions

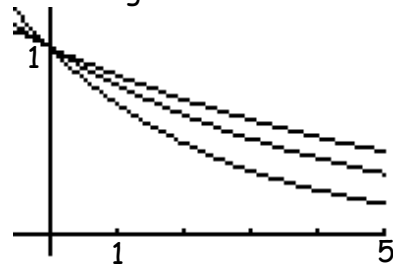
- 1.) The three exponential functions $y = 2^x$, $y = 3^x$, and $y = e^x$ are shown below. Which formula goes with which graph? **Explain** your reasoning.



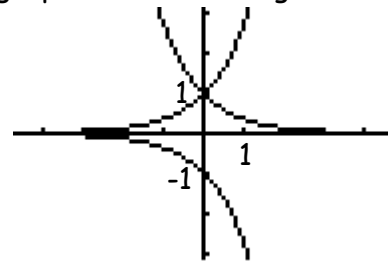
- 3.) The graphs of $y = e^x$, $y = 2e^x$, and $y = 3e^x$ are shown below. **Explain how** you can match these equations to their graphs **without** using a calculator.



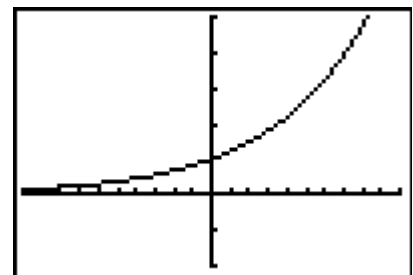
- 2.) The graphs of $f(x) = (0.7)^x$, $g(x) = (0.8)^x$, and $h(x) = (0.85)^x$ are shown below. **Explain how** you can match these equations to their graph **without** using a calculator.



- 4.) The graphs of $y = e^x$, $y = e^{-x}$, and $y = -e^x$ are shown below. you can match these equations to their graphs **without** using a calculator.

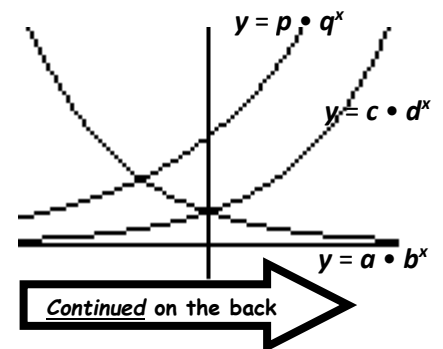


- 5.) Suppose you use your calculator to graph $y = 1.04^{5x}$. You correctly enter $y = 1.04^{(5x)}$, and see the graph shown to the right. A friend graphed the function by entering $y = 1.04^{5x}$ in his calculator and said, "The graph is a straight line, so I must have the wrong window." **Explain why** changing the window will **not** correct your friend's error.



Window: [-10,10] x [-2,5]

- 6.) Consider the exponential functions graphed to the right, and the six constants $a, b, c, d, p,$ and q .
- Which of these constants are **definitely** positive?
 - Which of these constants are **definitely** between 0 and 1?
 - Which of these constants **could** be between 0 and 1?
 - Which two of these constants are **definitely** equal?
 - Which one of the following pairs of constants **could** be equal?
 a and p b and d b and q d and q



Continued on the back →

7.) For which value(s) of a and b is $y = ab^x$ an **increasing** function? ... a **decreasing** function?

8.) The functions $f(x) = \left(\frac{1}{2}\right)^x$ and $g(x) = \frac{1}{x}$ are similar in that they both tend toward zero as x becomes large. Using your calculator, determine which function, f or g , approaches zero **faster**.

9.) List the specific transformations needed to transform the graph of $h(x) = 2^x$ into the graph of the given functions:

(a) $f(x) = 2^x - 5$

(b) $g(x) = 3(2^x)$

(c) $k(x) = 2^{x+2} - 5$

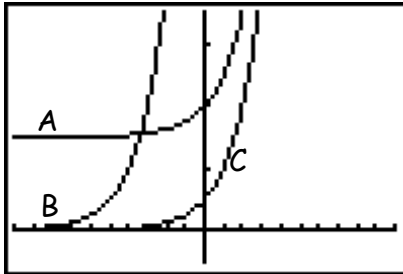
(d) $m(x) = -5(2^{x-1}) + 7$

10.) **Match** each of the following functions to the graphs shown below:

(a) $f(x) = b^x$

(b) $g(x) = b^x + 3$

(c) $h(x) = b^{x+5}$



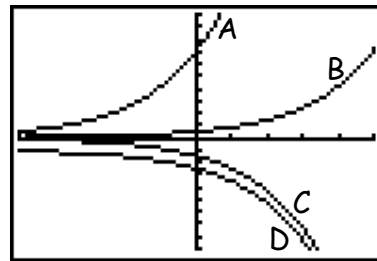
11.) **Match** each of the following functions to the graphs shown below:

(a) $f(x) = a^x$

(b) $g(x) = -3a^x$

(c) $h(x) = a^{x+5}$

(d) $k(x) = -3a^x - 2$



12.) Determine whether each of the following functions are **even** (symmetric across the y -axis), **odd** (rotational symmetry around the origin), or **neither**. (HINT: Look at the possible **symmetry** of their graphs.)

(a) $f(x) = 10^x$

(b) $g(x) = \frac{e^x + e^{-x}}{2}$

(c) $h(x) = e^{-x^2}$

13.) **Explain why** $e^x + e^{-x}$ is approximately equal to e^x when x is very large.

14.) The population of a colony of fruit flies t days from now is given by the function $P(t) = 100 \cdot 3^{t/10}$.

(a) What will the population be in 15 days? ... in 25 days?

(b) How many days will it take the population to reach 2500?

15.) A certain type of bacteria grows according to the function $f(t) = 5000 \cdot e^{0.4055t}$, where the time t is measured in hours.

(a) What will the population be in 8 hours?

(b) When will the population reach one million?